**Supplementary information**

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# **Bayesian estimation of gene constraint from an evolutionary model with gene features**

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## **A Empirical Bayes with** NGBoost

#### **Empirical Bayes overview**

In the simplest version of empirical Bayes, we specify the form of the prior distribution and assume that that prior is shared across all genes—for example, for gene *i* we might assume the prior distribution is  $s_{\text{het}}^{(i)} \sim \text{LogitNormal}(\mu, \sigma)$  with density  $p_{\mu, \sigma}(s_{\text{he}}^{(i)})$  $\lim_{\text{het}}$ ), where the LogitNormal $(\mu, \sigma)$  distribution is defined such that  $logit(s^{(i)}_{he})$  $\lambda_{\text{het}}^{(i)}$ ) =  $\log(s_{\text{he}}^{(i)})$  $\frac{(i)}{\text{het}} / (1 - s_{\text{he}}^{(i)}$  $\binom{U}{\text{het}}$ ) is normally distributed with mean *μ* and variance  $σ<sup>2</sup>$ . We can then estimate *μ* and *σ* using the observed LOF data for each gene,  $y_1, \ldots, y_M$ , by maximizing the marginal likelihood:

$$
\prod_{i=1}^M \int_0^1 p\left(\mathbf{y}_i \mid s_{\text{het}}^{(i)}\right) p_{\mu,\sigma}\left(s_{\text{het}}^{(i)}\right) \text{d}s_{\text{het}}^{(i)}.
$$

Next, we can compute the posterior distribution of  $s_{\text{het}}^{(i)}$  for each gene,

$$
p\left(s_{\text{het}}^{(i)} \mid \mathbf{y}_i\right) = \frac{p\left(\mathbf{y}_i \mid s_{\text{het}}^{(i)}\right) p_{\mu, \sigma}\left(s_{\text{het}}^{(i)}\right)}{\int_0^1 p\left(\mathbf{y}_i \mid s_{\text{het}}^{(i)}\right) p_{\mu, \sigma}\left(s_{\text{het}}^{(i)}\right) ds_{\text{het}}^{(i)}}.
$$

However, rather than learning the parameters for the prior from only the LOF data, we can also use gene features to learn gene-specific prior parameters, *µ<sup>i</sup>* and *σi*. To do this, we used a machine learning approach, NGBoost, to learn functions *f* and *g* such that  $\mu_i = f(\mathbf{x}_i)$  and  $\sigma_i = g(\mathbf{x}_i)$ , where  $x_i$  is a vector of gene features associated with gene *i*. In the next few sections, we will describe how we learned *f* and *g*.

#### NGBoost

NGBoost (Natural Gradient Boosting) is an approach for training gradient boosted trees to predict the parameters of a probability distribution [1]. Gradient boosted trees are a type of machine learning model typically used to predict outcomes *y*, from features *X*, producing point estimates such as predictions of **E**[*y | X*]; in contrast, NGBoost uses gradient boosted trees to predict *p*(*y |*  $X = x$ ) by learning parameters of  $p(y | X = x)$  as functions of x—in other words, NGBoost allows us to learn the full distribution of *y* conditioned on observing the features *x*.

Specifically, for gene *i*, we assume the prior distribution is  $s_{\text{het}}^{(i)} \sim \text{LogitNormal}(\mu_i, \sigma_i)$ , with density  $p_{\mu_i,\sigma_i}(s_{\text{he}}^{(i)})$  $\mathcal{L}_{\text{het}}^{(i)}$ ).  $\mu_i = f(\pmb{x}_i)$  and  $\sigma_i = g(\pmb{x}_i)$  are functions of the vector of gene features  $\pmb{x}_i$ , where *f* and *g* are parameterized as gradient-boosted trees. We chose this distribution as previous work has suggested that  $s_{\rm het}^{(i)}$  is distributed on a logarithmic scale [2–4], yet,  $s_{\rm het}^{(i)}$  is also bounded between 0 and 1. Both of these properties are enforced by the LogitNormal distribution. In Supplementary Note B, we develop a population genetic likelihood  $p(\bm{y}_i \mid s_{\text{he}}^{(i)})$  $\frac{d^{(1)}}{\partial x^{(1)}}$ , where  $y_i$  is a vector that represents the observed frequencies of each possible loss of function variant for the gene. Then, with *M* genes in the training set, the score that NGBoost minimizes during training is:

$$
\sum_{i=1}^{M} S\left(\mathbf{y}_{i}; \mu_{i}, \sigma_{i}\right) = -\sum_{i=1}^{M} \log p\left(\mathbf{y}_{i}\right) = -\sum_{i=1}^{M} \log \left(\int_{0}^{1} p\left(\mathbf{y}_{i} \mid s_{\text{het}}^{(i)}\right) p_{\mu_{i}, \sigma_{i}}\left(s_{\text{het}}^{(i)}\right) d s_{\text{het}}^{(i)}\right)
$$

.

To do this, NGBoost first initializes the parameters of *f* and *g* such that all genes have the same prior distribution. Next, NGBoost adopts a gradient descent approach to minimize the score function: for each iteration until training ends, NGBoost first computes the gradient of gene *i*'s score with respect to the parameters  $\mu_i$  and  $\sigma_i$  of  $p_{\mu_i,\sigma_i}(s_{\text{he}}^{(i)})$  $\frac{f(t)}{f(t)}$ . In the original implementation, NGBoost uses *natural gradients*, which take into account the underlying "information geometry" of the space of distributions in a way that standard gradients do not [5], but natural gradients are costly to compute, so we use standard gradients instead. After computing the gradient, NGBoost fits a decision tree to each dimension of the gradient, updating  $\mu_i$  and  $\sigma_i$  in the direction that most steeply decreases the gene's score. While gradient-boosting algorithms (including NGBoost, by default) typically fit a single decision tree at each iteration, we allow NGBoost to fit up to n\_estimators trees per iteration, where n\_estimators is a hyperparameter that we tune.

Below, we summarize the training algorithm. Let  $\mu_i^{(t)}, \sigma_i^{(t)}$  denote the parameters of the prior at training iteration *t*.

- 1. Initialize parameters for all genes,  $i = 1, ..., M$ :  $\mu_i^{(0)}$ ,  $\sigma_i^{(0)} = \text{argmin}_{\mu, \sigma} \sum_{i=1}^M S(\bm{y}_i; \mu, \sigma)$
- 2. For iterations  $t = 1, ..., T$ :
	- (a) For each gene, calculate gradients of the score:  $\nabla S\left(\mathbf{y_i}; \mu_i^{(t)}, \sigma_i^{(t)}\right)$ ), whose two components we denote as  $\nabla S_{\mu_i}$  and  $\nabla S_{\sigma_i}$
	- (b) Fit decision trees  $f^{(t)}$  and  $g^{(t)}$  on the gradients:  $f^{(t)} = \text{fit}\left(\left\{\mathbf{x}_i, \nabla S_{\mu_i}\right\}_{i=1}^M\right)$  $\overline{ }$

$$
g^{(t)} = \mathrm{fit}\left(\{\mathbf{x}_i, \nabla S_{\sigma_i}\}_{i=1}^M\right)
$$

(c) Perform a line search to find a scaling,  $\phi^{(t)}$  that optimizes the loss function along the search direction implied by  $f^{(t)}$  and  $g^{(t)}$ . That is, set:

$$
\phi^{(t)} = \operatorname{argmin}_{\phi} \sum_{i=1}^{M} S(\mathbf{y}_i; \mu_i^{(t-1)} - \phi f^{(t)}(\mathbf{x}_i), \sigma_i^{(t-1)} - \phi g^{(t)}(\mathbf{x}_i))
$$

In practice, NGBoost approximately solves this optimization problem by initializing at  $\phi = 1$ , iteratively doubling  $\phi$  until the objective begins to increase, and then restarting at  $\phi = 1$  and iteratively halving  $\phi$  until the objective begins to increase. Whichever of these  $\phi$  minimized the objective function is used for  $\phi^{(t)}.$ 

(d) Update the parameters for each gene, where *η* is a learning rate that is chosen by the user as a hyperparameter:

$$
\mu_i^{(t)} = \mu_i^{(t-1)} - \eta \phi^{(t)} f^{(t)}(\mathbf{x}_i)
$$

$$
\sigma_i^{(t)} = \sigma_i^{(t-1)} - \eta \phi^{(t)} g^{(t)}(\mathbf{x}_i)
$$

Once training is complete, we obtain a learned prior with parameters  $\mu_i^{(T)}$ ,  $\sigma_i^{(T)}$ , and can compute the posterior distribution of *s*het

$$
p\left(s_{\text{het}}^{(i)} \mid \mathbf{y}_i\right) = \frac{p\left(\mathbf{y}_i \mid s_{\text{het}}^{(i)}\right) p_{\mu_i^{(T)} , \sigma_i^{(T)}}\left(s_{\text{het}}^{(i)}\right)}{p\left(\mathbf{y}_i\right)}
$$

as well as the mean of this distribution

$$
\mathbb{E}\left[s_{\text{het}}^{(i)} \mid \boldsymbol{y}_i\right] = \int_0^1 s_{\text{het}}^{(i)} p(s_{\text{het}}^{(i)} \mid \boldsymbol{y}_i) \text{d}s_{\text{het}}^{(i)}
$$

To compute 95% Credible Intervals, we compute the CDF of the posterior distribution using Pytorch's cumulative\_trapezoid function [6]. Then, the 95% Credible Interval per gene is defined as  $[\text{lb}^{(i)}, \text{ub}^{(i)}]$  such that  $P(s_{\text{het}}^{(i)} < \text{lb}^{(i)}) = 0.025$  and  $P(s_{\text{het}}^{(i)} < \text{ub}^{(i)}) = 0.975$ .

#### NGBoost**— implementation details**

To initialize parameters (step 1 in the training algorithm), we perform gradient descent with the AdamW optimizer [7] implemented in PyTorch [6] with a learning rate of  $1 \times 10^{-3}$  and otherwise default settings. We initialize the optimization at  $\mu = 0$  and  $\sigma = 1$ .

We numerically compute all integrals using the trapezoid method implemented in PyTorch, which enables gradient computation through automatic differentiation. We perform all integrals using the transformed parameter, Logit(*s*het). Since *s*het has a LogitNormal prior, this transformation has a Normal distribution, and hence puts all but a negligible fraction of its mass within 8 standard deviations,  $\sigma$ , of its mean,  $\mu$ . Therefore, we perform the trapezoid method on an evenly spaced grid of 10<sup>4</sup> points on the domain  $\mu - 8\sigma$ ,  $\mu + 8\sigma$ .

To flexibly fit decision trees at each training iteration, we use the XGBoost package, a library used for fitting standard gradient boosted trees [8]. In comparison to the default NGBoost learner, XGBoost supports missing features and allows for adjustment of numerous hyperparameters (see "Training and Validation" in Methods). In contrast to typical applications of XGBoost, we only allow a few (n\_estimators in Supplementary Table 6) trees to be fit at each training iteration, as we are using XGBoost within a training loop rather than as a standalone approach for model fitting.

All distributions were implemented using PyTorch, and training was conducted with GPU support when available, with tree\_method = "gpu\_hist" for the XGBoost learners.

## **B Population Genetics Model**

#### **Overview of model**

Some of the most commonly used measures of gene constraint (pLI [9], LOEUF [10]) are framed in terms of the number of unique LOFs observed in gene, *O*, relative to the number expected under a null model, *E*. While operationalizing constraint as some function of *O* and *E* captures the intuition that seeing fewer LOFs than expected is evidence that a gene is conserved, the numerical values of pLI and LOEUF are difficult to interpret. In practice this means that such measures can be useful for ranking which genes are important, but it makes it difficult to contextualize these results in terms of other types of variants, such as missense or noncoding variants, or copy number variants. Previous approaches have pioneered using a population genetics model in this context to obtain interpretable estimates, albeit with different technical details that we discuss below [2–4].

In order to obtain a more interpretable measure of constraint, we formalize constraint as the strength of natural selection acting against gene loss-of-function in a population genetics model. That is, we can ask how much fitness is reduced on average for an individual with one or two nonfunctional copies of a gene relative to individuals with two functional copies, following previous work [2–4]. To tie this concept of constraint to observed allele frequency data, we use a slightly simplified version of the discrete-time Wright Fisher model. This model contains mutation, selection, and genetic drift, and assumes that there are only two alleles and that the population is panmictic, monoecious, and has non-overlapping generations. While all of these assumptions are violated in humans (there are four nucleotides, population structure, two sexes, and overlapping generations), the model still provides a good approximation to allele frequency dynamics through time. If the allele frequency in generation  $k$  is  $f_k$ , then we model the allele frequency in the next generation via binomial sampling:

$$
2N_{k+1}f_{k+1} \sim \text{Binomial}\left(2N_{k+1}, p\left(f_k\right)\right),\tag{1}
$$

where  $N_{k+1}$  is the number of diploid individuals in generation  $k + 1$ , with

$$
p(f_k) := \frac{(1 - s_{\text{het}})\widetilde{f}_k \left(1 - \widetilde{f}_k\right) + (1 - s_{\text{hom}})\widetilde{f}_k^2}{\left(1 - \widetilde{f}_k\right)^2 + 2(1 - s_{\text{het}})\widetilde{f}_k \left(1 - \widetilde{f}_k\right) + (1 - s_{\text{hom}})\widetilde{f}_k^2},
$$

where  $f_k = f_k(1 - \mu_{1 \to 0}) + \mu_{0 \to 1}(1 - f_k)$  is the allele frequency after alleles change from non-LOF to LOF at rate  $\mu_{0\to1}$  and from LOF to non-LOF at rate  $\mu_{1\to0}$ . The function  $p(\cdot)$  arises from considering bidirectional mutation and approximating a model of diploid selection where the relative reproductive success of individuals with 0, 1, or 2 copies of the LOF are 1, 1 − *s*het, and 1 − *s*hom respectively [11]. In practice, most LOF variants are extremely rare, and so it is exceedingly unlikely to find individuals homozygous for the LOF. This makes estimating *s*hom as a separate parameter very difficult, and so we instead assume that  $s_{\text{hom}} = \min \{2s_{\text{het}}, 1\}$ . This is equivalent to assuming genic selection (i.e., additive fitness effects) with the constraint that an individual's relative fitness cannot be lower than 0.

Equation 1 fully specifies the model except for an initial condition. That is, we need to know what the distribution of frequencies is in generation 0. One mathematically appealing choice would be to assume that the population is at equilibrium at time 0, but this seemingly straightforward choice results in nonsensical conclusions. To see why, if the mutation rates are low and selection is negligible, then at equilibrium, with extremely high probability the population will either be in a state where the frequency of the LOF allele is very close to zero or in a state where the frequency of the LOF allele is very close to one. If the mutation rates between the two alleles are close to equal, then these two cases happen roughly equally often. That is, we would expect there to be a ∼50% chance that the population is fixed or nearly fixed for the LOF mutation. If there are multiple independently evolving sites at which a LOF could arise (or if there are many more ways to mutate to a LOF state than a non-LOF state), then the chance that any of these sites is fixed or nearly fixed for a LOF rapidly approaches 100%. Under this equilibrium assumption, we thus reach the absurd conclusion that the mere act of observing a gene that is functional in a majority of the population is overwhelming evidence that the gene is strongly selected for. Another way of viewing this is that in reality we can only observe genes that are functional in an appreciable fraction of the population, and so we should somehow be conditioning on this event, whereas the equilibrium assumption looks at a given randomly chosen stretch of DNA and asks whether it could be a gene given some set of mutations. Indeed, any randomly chosen stretch of DNA could be made a gene through a series of mutations, but for any given stretch it would be extremely unlikely to be a functional gene, and the equilibrium assumption exactly captures how rare this would be.

We instead use the equilibrium of another process as the initial condition, which avoids these conceptual pitfalls. We assume the distribution of frequencies at generation 0 is the equilibrium conditioned on the LOF allele never reaching fixation in the population. We then compute the likelihood of observing a given present-day frequency while continuing to condition on non-fixation of the LOF allele. This assumption implies that no matter the current frequency of the LOF variant, we know that at some point in the past the population was fixed for the functional version of the gene, and the LOF variant can thus be thought of as being "derived" and the non-LOF variant "ancestral". In the limit of infinitely low (but non-zero) mutation rates, this assumption becomes equivalent to the commonly assumed "infinite sites" model commonly used to compute frequency in population genetics [12]. In contrast to the infinite sites model, where the probability that any given site is segregating must be 0, our model allows us to compute the probability that a given site is segregating. Furthermore, we can easily model recurrent mutation which can be important for sites with large mutation rates (such as CpGs) and large sample sizes [13], whereas under the infinite sites model each mutation necessarily happens at a unique position in the genome, ruling out the possibility of recurrent mutation. Below, we will write  $p_{\text{DTWF}}(y \mid s_{\text{het}})$  for the probability mass function computed using this procedure, with "DTWF" representing Discrete-Time Wright-Fisher, and *y* being an observed LOF allele frequency.

Equation 1 is easy to describe and simulate under, and a very similar model has been used in an approximate Bayesian computation approach to estimate *s*het [4]. While simulation is easy, computing likelihoods under this model is difficult for large sample sizes, and unfortunately we need explicit likelihoods in our empirical Bayes approach. In recent work [14], we have developed an efficient method for computing likelihoods under this model. The key idea is that the above dynamics can be written as

$$
\mathbf{v}_{k+1} = \mathbf{M}_k^T \mathbf{v}_k
$$

where  $\mathbf{v}_k$  is a vector of dimension  $2N + 1$  where entry *i* is the probability that there are *i* haploids

that have the LOF allele in generation  $k$ , and  $M_k$  is a matrix where row *i* is the the probability mass function of the Binomial distribution in Equation 1 given that the allele frequency in generation *k* is *i*/2*Nk*. This formulation makes clear that we can obtain the likelihood of observing a given frequency at present given some initial distribution by performing a series of matrix-vector multiplications. Naively this would be prohibitively slow as  $M_k$  can be as large as  $10^7 \times 10^7$ , but in [14] we show that  $M_k$  is approximately highly structured — it is both approximately extremely sparse and approximately extremely low rank. Combining these insights we can perform matrix-vector multiplication that is provably accurate while reducing the runtime for matrix-vector multiplication from  $O(N_k^2)$  to  $O(N_k)$ . Similar insights can be used to speed up the computation of equilibria, which we discuss in detail in [14]. Furthermore, as discussed above, we actually want to compute likelihoods conditioned on non-fixation of the LOF allele, but that is as simple as setting the column of  $M_k$  corresponding to fixation to 0, and then renormalizing **v**. We precompute these likelihoods for each possible pair of mutation rates (to and from the LOF allele) across a range of *s*het values (100 log-linearly spaced points between 10−<sup>8</sup> and 1, as well as 0). We describe how we set the mutation rates and the population sizes implicit in  $M_k$  below.

#### **Modeling misannotation of LOFs**

Under the likelihood described above, and as seen in Fig. 2**A**, positions where a LOF variant could occur, but no LOF alleles are observed are slight evidence in favor of selection, while high frequency variants are extremely strong evidence against selection. Meanwhile, we suspect that many variants that are annotated as causing LOF actually have little to no effect on the gene product due to some form of misannotation. If these misannotated variants evolve effectively neutrally, they can reach high frequencies and cause us to artifactually infer artificially low levels of selection. These misannotated variants can be particularly problematic for approaches that combine frequencies across all LOFs within a gene to obtain an aggregate gene-level LOF frequency [2–4].

LOEUF [10] and pLI [9] avoid this problem by throwing away all frequency information except for whether a LOF is segregating or not. While this approach is more robust, the ignored frequency information is extremely useful for estimating the strength of selection. For example, consider a gene where we expect to see 5 unique LOFs under neutrality and we see 3 segregating LOFs. This might seem like weak or negligible constraint  $(O/E = 0.6)$ , but if those 3 sites are all highly mutable and the variants at those sites are each only present in a single individual, then it is plausible that this gene is quite constrained.

To take full advantage of the information in the LOF frequencies while remaining robust to misannotation, we take a composite likelihood approach [15], closely related to the Poisson random field assumption commonly used in population genetics [12]. We approximate gene-level likelihoods as a product of variant level likelihoods

$$
p^{(i)}\left(\mathbf{y}^{(i)} \mid s_{\text{het}}^{(i)}\right) \approx \prod_{j=1}^{J_i} p_{\text{variant}}\left(\mathbf{y}_j^{(i)} \mid s_{\text{het}}^{(i)}\right),
$$

where  $y^{(i)}$  is a vector of the observed allele frequencies at each possible LOF site in gene *i*, and  $s_{\rm het}^{(i)}$  is the selection coefficient for having a heterozygous loss-of-function of gene *i*. Under this formulation, we can easily model misannotation by assuming that each LOF independently has some probability of being misannotated,  $p_{miss}$ , and that misannotated variants evolve neutrally:

$$
p_{\text{variant}}\left(\mathbf{y}_{j}^{(i)} \mid s_{\text{het}}^{(i)}\right) = (1 - p_{\text{miss}}) p_{\text{DTWF}}\left(\mathbf{y}_{j}^{(i)} \mid s_{\text{het}}^{(i)}\right) + p_{\text{miss}} p_{\text{DTWF}}\left(\mathbf{y}_{j}^{(i)} \mid 0\right).
$$

Using this formulation, we can take full advantage of the rich information included in the exact sample frequencies of each LOF variant, while still being robust to occasional misannotation. In practice, we precompute  $p_{\text{variant}}$  using a grid of  $p_{\text{miss}}$  values, and then to obtain the likelihood at arbitrary values of *s*het and *p*miss we linearly interpolate in log-likelihood space. Below, we discuss our approach for setting  $p_{\text{miss}}$ .

Given a probability of misannoation, we can then calculate a posterior probability that any given variant has been misannotated. We include a table of these misannotation probabilities for all possible LOFs in [16].

Supplementary Fig. 1 shows the impact of modeling misannotation on the variant-level likelihoods. In particular we present the likelihood curves for individual variants of different frequencies at a high mutation rate site (analogous to Fig. 2**A**). We see that increasing *p*miss affects the likelihoods in two ways. First, it slightly flattens the overall likelihood, which makes sense as some information must be lost as we assume more and more LOFs are misannotated. Second, including *p*miss results in a floor on how low the likelihood can go, and higher values of *p*miss result in higher floors. This also makes sense, as any individual variant can always be "explained away" by it being misannotated, and in particular, the likelihood can never be lower than *p*miss times the likelihood of the variant under neutrality.

Supplementary Fig. 2 shows the impact of  $p_{\text{miss}}$  on gene-level likelihoods for two example genes. For *AARD*, a gene with only 4.3 expected LOFs and only one observed LOF,  $p_{\text{miss}}$  has a large impact on the log-likelihood. For low values of  $p_{\text{miss}}$  the single segregating LOF (present at a frequency of 42/250,000) provides enough evidence to strongly rule out *s*het *>* 0.02, with the likelihood rapidly approaching zero. In contrast, if there were no LOFs, then the likelihood would monotonically increase to a maximum at  $s_{\text{het}} = 1$ . As such, as  $p_{\text{miss}}$  increases, we start to see bimodal likelihoods, due to being a mixture of the case where the segregating variant is not misannotated (where the likelihood would be monotonically decreasing), and the case where the segregating variant is misannotated (where the likelihood would be monotonically increasing). For *LPA*, which has 90.2 expected LOFs and 118 observed LOFs, there are enough variants of similar frequencies where even for  $p_{\text{miss}}$  as high as 0.1 it is unlikely for all of the LOFs to be due to misannotation. As a result, the likelihood is relatively insensitive to  $p_{\text{miss}}$ , with  $p_{\text{miss}}$  primarily acting to slightly flatten the likelihood.

We also investigated whether the inferred posterior probabilities of misannotation vary based on their positions within transcripts. We mapped each LOF to its position relative to the start and end of the canonical transcript for each gene. We found that LOFs due to early stop codons are inferred to be more likely to be misannotated if they are near the start or end of transcripts, possibly due to alternative translation initiation [17] or avoiding the nonsense-mediated decay pathway [18] respectively. In contrast, variants that are annotated as LOFs due to having a predicted effect on splicing are increasingly likely to be misannotated toward the end of transcripts. These results are presented in Supplementary Fig. 3.

As an example of the importance of correcting for misannotation, we consider the case of the gene *PPFIA3* (ENSG00000177380). This gene has a LOEUF score of 0.12 and so appears very constrained, but in an early version of our model where we did not incorporate variant misannotation, we inferred a posterior mean value of  $s_{\text{het}}$  of  $\sim$ 2 × 10<sup>-4</sup>, which is right at the border of being nearly neutral. Inspecting the LOF data for this gene, we find that all potential LOFs are either not observed or observed in a single individual, except for a single splice donordisrupting variant at 16% frequency. There are no obvious signs indicating that this variant is misannotated (e.g., in terms of coverage or mappability). If we model misannotation, however, we find that this variant is likely misannotated (posterior probability of misannotation ∼100%), and as a result we estimate extremely strong selection against gene loss-of-function (posterior mean *s*het of ∼ 0.202). Indeed, a single autosomal dominant missense variant in this gene is suspected to have caused a number of severe symptoms including developmental delay, intellectual disability, seizures, and macrocephaly in an Undiagnosed Diseases Network participant (https://undiagnosed.hms.harvard.edu/participants/participant-159/) [19].

#### **Modeling the X chromosome**

We must slightly modify our model when applying it to the X chromosome. Because males only have one copy of the X chromosome, there are only 3/4 as many X chromosomes as autosomes (assuming an approximately equal sex ratio). As a result, when dealing with the X chromosome we scale all population sizes to 3/4 of the size used for the autosomes (rounded to the nearest integer). We also need to slightly modify the expected frequency in the next generation. We assume haploid selection in males with strength *s*hom, and diploid selection in females with selection coefficients *s*het and *s*hom for individuals heterozygous and homozygous for the LOF variant respectively. This selection results in modified allele frequencies in the pool of males and females, and the we assume that each chromosome in the next generation has  $1/3$  probability of coming from a male, and 2/3 probability of coming from a female. This means that the expected frequency in the next generation is 1/3 times the post-selection frequency in males plus 2/3 times the post-selection frequency in females. Variants within the pseudoautosomal regions on the X are modeled identically to variants on the autosomes. Agarwal and colleagues also considered selection on the X in the context of LOF variants, with a model similar to that described here [4].

#### **Model parameters**

Our model has three key parameters — the mutation rate, the demographic model (i.e., population sizes through time), and the probability that different variants are misannotated.

We obtained mutation rates from gnomAD [10, Supplementary Dataset 10], which take into account trinucleotide context and methylation level (for CpG to TpG mutations). In our population genetics model, we assume that there are only two alleles (a functional allele and a LOF allele), whereas in reality there are four nucleotides. We approximate the rate of mutating from the functional allele to the LOF allele as being the sum of the mutation rates from the reference nucleotide to any nucleotide that might result in LOF. For example, if the reference allele is A, and either a C or a T would result in LOF, then we say that the rate at which the functional allele mutates to the LOF allele is the rate at which A mutates to C in this context plus the rate at which A mutates to T in this context. For the rate of back mutation from the LOF allele to the functional allele, we compute a weighted average of the rates of each possible LOF nucleotide back-mutating to any possible non-LOF nucleotide, weighed by the probability that the original non-LOF nucleotide mutated to that particular LOF nucleotide. Continuing our previous example, suppose A mutates to C at rate  $1 \times 10^{-8}$  and A mutates to T at a rate  $1.5 \times 10^{-8}$ . Then conditioned on there having been a single mutation resulting in a LOF variant, there is a  $1/2.5 = 0.4$  chance that the LOF is C and 0.6 chance that the LOF is T. We then compute the back mutation rate as 0.4 times the rate at which C mutates to A in this context plus the rate at which C mutates to G in this context (since both A and G do not result in LOF) plus 0.6 times the rate at which T mutates to A in this context plus the rate at which T mutates to G in this context. Implicitly this scheme assumes that the flanking nucleotides in the trinucleotide context do not change, and we further assume that all mutations resulting in CpGs result in unmethylated CpGs.

For the population sizes in each generation, we used the "CEU" model inferred in [20] using the 1000 Genomes Project data [21]. This model was also used in [4]. Population sizes under this model are relatively constant before 5156 generations ago (approximately 155 thousand years ago) and the effects of strong selection are relatively insensitive to all but the most recent population sizes, so for a computational speedup we assumed that the population size was constant prior to 5156 generations ago. Recently, [4] found that this CEU model underestimates the number of low frequency variants and that changing the population size to 5,000,000 for the most recent 50 generations provides a better fit to the data. We used both demographic models and found qualitatively similar results, with slightly better fit provided by the modified model, so we used that demographic model for all subsequent analyses. In both cases, we modified the most ancient population sizes, which are relatively constant, to be actually constant to speed up likelihood calculations. The demographic models are presented in Supplementary Fig. 4.

Given that demography plays an important role in the likelihood and that gnomAD contains individuals of diverse ancestries, we wanted to make sure that our results were generally robust to misspecification of the demography. All of the results presented in the main text used the entirety of gnomAD v2, but we also trained models using the subset of individuals labeled in the dataset as "non-Finnish European" (NFE) as well as all non-NFE individuals. When training these models we assumed the Agarwal. *et al.* demography, regardless of the ancestry of the individuals used in training. The posterior mean *s*het values under all three models are quantitatively and qualitatively consistent, with Spearman correlations greater than 0.93 between all pairs (Extended Data Fig. 2). The high concordance indicates that our pooling of individuals of different genetic ancestries is justified, and that our results are robust to slight mismatches between the demography and the individuals used.

The only remaining model parameter is  $p_{\text{miss}}$  the probability that any given LOF is misannotated. Throughout we focus on LOFs that either introduce early stop codons, disrupt splice donors, or disrupts splice acceptors. Given that predicting which variants have these different consequences involves different bioinformatic challenges, we inferred separate misannoatation probabilities  $p_{\text{miss}}^c$  for  $c \in \{\text{stop codon, splice donor, splice acceptor}\}\.$  Below we write  $p_{\text{miss}}$  for the collection of these three misannotation parameters. To get a rough estimate of these parameters and avoid excessive computational burden, we took an h-likelihood approach [22,23]. That is, we jointly maximized the likelihood across all genes with respect to their selective constraints as well as the the three misannotation probabilities that are shared across all genes:

$$
\max_{p_{\text{miss}},s_{\text{het}}^{(1)},\ldots,s_{\text{het}}^{(M)}}\sum_{i=1}^{M}\log p\left(\mathbf{y}^{(i)} \mid s_{\text{het}}^{(i)} p_{\text{miss}}\right).
$$

This approach of just using the maximum likelihood estimates of *s*het for each gene contrasts with the standard empirical Bayes approach, which would involve marginalizing out the unknown *s*het values. Yet, this marginalization step depends on the prior on *s*het, which we learn via our NGBoost framework. As a result, we would need to repeatedly run our NGBoost framework as an inner loop to perform the standard empirical Bayes approach on  $p_{\text{miss}}$ . For our application, these values are nuisance parameters, and the results are relatively insensitive to their exact values so we opted for this simpler h-likelihood approach. Ultimately, we estimate that the probability of misannotation is 0.7%, 4.5%, and 8.1% for stop codons, splice donors, and splice acceptors respectively.



Supplementary Fig. 1: **Dependence of likelihoods on parameters.** *Relative log likelihoods for a high mutation rate site with different allele frequencies, f , and misannotation probabilities, pmiss.*



Supplementary Fig. 2: **Likelihoods for example genes.** *Relative log likelihoods (top row) or scaled likelihoods* (bottom row) for representative genes AARD (left column) and LPA (right column) for different misannotation probabilities,  $p_{miss}$ . Here we set  $p_{miss}$  to be the same regardless of the type of LOF variant. AARD is a representative example of a gene with few expected LOFs, while LPA is a representative example of a gene with many expected LOFs.



Supplementary Fig. 3: **Mean posterior probabilities of misannotation along canonical transcripts.** *Each* potential LOF was mapped to its position within the transcript normalized to the total transcript length. Variants within the first 5% of the transcript were binned, and then the next 5% of the transcript, and so on. We subsampled the number of variants of each type within each bin to match the bin with the fewest variants of that type. This resulted in  $n = 79,160$  early stop codon pLOFs per bin and  $n = 15,146$  splice disrupting pLOFs per bin. In the plot, points represent the mean of the inferred posterior probabilities within each bin, and lines correspond to  $\pm 1.96$  standard *errors of the mean estimate.*



Supplementary Fig. 4: **Comparison of CEU demographies.** *CEU demography inferred by Schiffels and Durbin [20], modified by Agarwal and colleagues [4], and further modified for this paper.*

# **C Feature processing and selection**

We compiled 10 types of gene features from several sources:

- 1. *Gene structure.* Gene structure features were derived from GENCODE gene annotations (Release 39) [24]. Such features include the number of transcripts and, for the primary transcript of each gene (the transcript tagged Ensembl\_canonical), the number of exons as well as the length and GC content of the transcript, total coding region, 5' UTR, and 3' UTR.
- 2. *Gene expression.* We used gene features from 77 bulk and single-cell RNA-seq datasets, processed and derived in [25]. These datasets can be grouped into 24 categories representing tissues, cell types, and developmental stage (Supplementary Table 3). For each dataset, features were derived separately from all data and from individual cell clusters (for example, gene loadings on principal components). In addition, features were derived from comparisons between clusters (for example, t-statistics for differential expression). Finally, we include a metric, *τ*, that summarizes the tissue-specificity of gene expression [26].
- 3. *Biological pathways and Gene Ontology terms.* First, we included previously curated biological pathway features [25, 27]. In addition, to include GO terms that capture additional known relationships between genes, we downloaded Biological Pathway (BP), Molecular Function (MF), and Cellular Component (CC) terms [28] with at least 10 member genes using the procedure described in [29]. Features for each gene were encoded as binary indicators of the gene's membership in the pathways and GO terms.
- 4. *Connectedness in protein-protein interaction (PPI) networks.* We included previously computed measures of the connectedness of protein products of genes in PPI networks [29]. Connectedness was calculated as the number of interactions per protein weighted by the interaction confidence scores.
- 5. *Co-expression.* First, we included previously computed measures of the connectedness of genes in co-expression networks [29], where connectedness measures the relative number of neighbors of each gene in the network, averaged over tissues. Next, for each gene, we derived features representing its co-expression with other genes (i.e. correlation in their expression levels across samples). To do this, we downloaded from the GeneFriends database a co-expression network derived from GTEx RNA-seq samples [30, 31], calculated the variance in the co-expression for each gene, and kept the 6,000 most variable genes. Then, we included the co-expression with each of these 6,000 genes as a feature.
- 6. *Gene regulatory landscape.* Gene regulatory features include the counts and properties of the enhancers and promoters that regulate each gene. First, we included the number of promoters per gene estimated by the FANTOM consortium using Cap Analysis of Gene Expression [29, 32]. Next, for each gene, we calculated the number, summed length, and summed score of enhancer-to-gene links predicted using the Activity-By-Contact (ABC) approach [33, 34], where an enhancer is considered linked to a gene if its ABC score is  $\geq$ 0.015. We computed separate features for each of 131 biosamples. We also included features derived by aggregating over all biosamples for both ABC enhancers and predicted enhancers from the Roadmap Epigenomics Consortium [29, 35, 36]—these feature include the number

of biosamples with an active enhancer element, the total number of enhancer elements, the total number of enhancer elements after taking merging enhancer domains, the total length of the merged domains, and the average total enhancer length in an active cell type. Finally, we included the enhancer-domain score for each gene [37] as a feature.

- 7. *Conservation across species.* For each gene, we calculated the mean and 95th percentile phast-Cons scores over the gene's exons for multiple alignments of 7, 17, 20, 30, and 100 vertebrate species to the human genome [38]. We downloaded phastCons Scores from https:// hgdownload.soe.ucsc.edu/goldenPath/hg38/. In addition, we included the fraction of coding sequence (CDS) or exons constrained across 240 mammals or 43 primates sequenced in the Zoonomia project [39], with constraint defined by the per-base phyloP [40] or phastCons score. Zoonomia data were downloaded from https://figshare.com/articles/dataset/ geneMatrix/13335548.
- 8. *Protein embedding features.* We included as features the embeddings learned by an autoencoder(ProtT5) trained on protein sequences [41]. Embeddings were downloaded from https: //zenodo.org/record/5047020. The embedding for each protein is a fixed-size vector that captures some of the protein's biophysical and functional properties. For each gene with more than one protein product, we averaged the embeddings of the proteins for that gene.
- 9. *Subcellular localization.* We included as features the subcellular localization of each protein and whether the protein is membrane-bound or soluble, as predicted by deep neural networks trained on the ProtT5 protein embeddings [41, 42]. Possible subcellular classes included nucleus, cytoplasm, extracellular space, mitochondrion, cell membrane, endoplasmatic reticulum, plastid, Golgi apparatus, lysosome or vacuole, and peroxisome. Predictions were one-hot encoded, and for each gene with more than one protein product, we summed the predictions for the gene's proteins. Predictions were downloaded from https: //zenodo.org/record/5047020.
- 10. *Missense constraint.* We included a measure of each gene's average intolerance to missense variants (UNEECON-G score) [43]. UNEECON-G scores incorporate variant-level features to account for differences in the effects of missense variants on gene function.

In addition to these 10 groups of features, we included a binary indicator for whether the gene is located on the X chromosome. Genes in the pseudoautosomal regions were categorized as autosomal.

After compiling these features (total of 65,383), we performed feature selection to minimize the practical complexity of training on such a large feature set and the complexity of the resulting model. First, we removed features with zero variance and features where the Spearman correlation of the feature values with *O*/*E* (the ratio of observed over expected unique LOF variants, computed using gnomAD data) was less than 0.1 or had a nominal p-value  $\geq$  0.05. Next, we performed simultaneous feature selection and an initial round of hyperparameter tuning using the shap-hypetune package, which uses Bayesian optimization to identify a set of features and hyperparameters that minimize the loss of a machine learning model fit on the training data. Specifically, we fit gradient-boosted trees using XGBoost to predict *O*/*E* from the gene features; we chose to perform feature selection using XGBoost rather than NGBoost as training XGBoost models is substantially faster, and because we expect features/hyperparameters that perform well for XGBoost

to also perform well for NGBoost. For each set of hyperparameters, shap-hypetune performs backward step-wise selection by removing the  $k$  least influential features (we chose  $k = 1000$  and calculated influence using SHAP scores) at each step. Finally, we performed further feature selection using shap-hypetune by fixing the hyperparameters and performing backward step-wise selection with  $k = 50$ . Ultimately, we included 1,248 features in the model.

# **D Potentialfor bias from the use of missense constraint or cross-species conservation**

In theory, features that correlate with patterns of human LOF polymophism but not with constraint may bias our estimates. In particular, a number of population genetic forces beyond natural selection contribute to patterns of conservation across species and missense constraint, and if these forces also affect observed LOF frequencies, then these features could be problematic. While we take into account mutation rate differences due to trinucleotide context and methylation status when considering LOFs, larger-scale variation in mutation rates and other forces that might alter the "local effective population size" could affect various measures of constraint as well as LOF frequency in a manner independent of selection.

To evaluate this possibility, we trained a model excluding missense constraint and cross-species conservation features, and compared the *s*het estimates from this model to those from the full model (Extended Data Fig. 1). We find that the posterior mean values of  $s_{\text{het}}$  are highly correlated between the models (Extended Data Fig. 1A, Spearman  $\rho = 0.92$ ). In addition, the performance of the models in classifying genes essential *in vitro* and in classifying developmental disorder genes is extremely similar (Extended Data Fig. 1**B**,**C**). These results indicate that the use of such features does not substantially bias the model.

## **E Estimating additional gene properties using GeneBayes**

GeneBayes is a flexible framework that can be used to infer other gene-level properties of interest beyond *s*het. In Fig. 6, we presented a schematic of the key components of GeneBayes that users should specify, which we describe in more detail now.

First, users should specify the gene features to use as predictors. We expect the gene features we use for *s*het estimation to work well for other applications, but GeneBayes supports any choice of features. In particular, GeneBayes can handle categorical and continuous features without feature scaling, as well as features with missing values.

Next, users should specify the form of the prior distribution. GeneBayes supports the distributions defined by the distributions package of PyTorch. GeneBayes also supports custom distributions, as long as they implement the methods used by GeneBayes (i.e. log\_prob and sample) and are differentiable within the PyTorch framework.

Finally, users need to specify a likelihood function that relates their gene property of interest to observed data. The likelihood can be specified in terms of a PyTorch distribution, or as a custom function.

After model training, GeneBayes outputs a per-gene posterior mean and 95% credible interval for the property of interest. For each parameter in the prior, GeneBayes also outputs a metric for each feature that represents the contribution of the feature to predictions of the parameter.

In the next section, we describe in more detail the two example applications that we outlined in Fig. 6.

### **Example applications**

#### **Differential expression**

In this example, users have estimates of log-fold changes in gene expression between conditions and their standard errors from a differential expression workflow, and would like to estimate logfold changes with greater power (e.g. for lowly-expressed genes with noisy estimates).

*Likelihood* We define  $\ell_{\rm DE}^{(i)}$  and  $\ell_i$  as the estimated and true log-fold change in expression respectively for gene *i*, and  $s_i$  as the standard error for the estimate. Then, we define the likelihood for  $\ell_i$ as

$$
\ell_{\rm DE}^{(i)} \mid \ell_i \sim \text{Normal}(\ell_i, s_i^2).
$$

*Prior* We describe two potential priors that one may choose to try. The first is a normal prior with parameters  $\mu_i$  and  $\sigma_i$ :

$$
\ell_i \sim \text{Normal}(\mu_i, \sigma_i^2).
$$

The second is a spike-and-slab prior with parameters  $\pi_i$ ,  $\mu_i$ , and  $\sigma_i$ , which assumes that gene *i* 

only has a  $\pi$ <sup>*i*</sup> probability of being differentially expressed:

$$
z_i \sim \text{Bernoulli}(\pi_i)
$$
  

$$
\ell_i | z_i \sim \begin{cases} 0, & \text{if } z_i = 0 \\ \text{Normal}(\mu_i, \sigma_i^2), & \text{if } z_i = 1 \end{cases}
$$

#### **Variant burden tests**

In this example, users have sequencing data from patients with a disease or (if calling *de novo* mutations) sequencing data from family trios, and would like to identify genes with excess mutational burden in patients (e.g. an excess of missense or LOF variants). One approach is to infer the relative risk for each gene (denoted as *γ<sup>i</sup>* for gene *i*), defined as the expected ratio of the number of variants in patients to the number of variants in healthy individuals.

*Likelihood* Let  $E_i$  be the number of variants we expect to observe for gene  $i$  given the study sample size and sequence-dependent mutation rates (e.g. expected counts obtained using the mutational model developed by [44]). Next, let *Oi* be the number of variants observed in patients for gene *i*. Then, we define the likelihood for *η<sup>i</sup>* as

$$
O_i | \eta_i \sim \text{Poisson}(\eta_i E_i).
$$

*Prior* Because *η<sup>i</sup>* is non-negative, one may want to choose a gamma prior with parameters *α<sup>i</sup>* and *βi*:

$$
\eta_i \sim \text{Gamma}(\alpha_i, \beta_i).
$$

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